# Central Bank Accounts For All! 

(And when they do any good.)

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## Motivation

## Why talk about it?

- Digital currency issued by central bank could effectively work as central bank account for all.
- Current policy interest (BIS, Bank of England, Bank of Canada, Swedish Riksbank)
- Besides $100 \%$ Reserve Banking way to prevent banks form creating money.
- Benes Kumhof (2012) argue 100\% reserve banking is the same as CBDC.
- Referendum in Switzerland ("Vollgeld").
- Debate in Icelandic parliament.
- "Chicago Plan" as response to banking crisis in 1930s.


## Motivation

The version of CBDC in this paper:

- Government only guarantees CBDC with capacity to tax, not deposits at banks.
- Government receives deposits from households, and hands them over to banks.


## Literature

## Who else talks about it?

- Setting the stage.
- Brunnermeier and Niepelt (2019).
- Central bankers.
- Coeure and Loh (2019), Engert and Fung (2017)
- People not primarily concerned about banks' incentives.
- Piazzesi and Schneider (2020), Bech and Garratt (2017), Chapman Wilikns (2018), Andolfatto (2018), Keister and Sanches (2019)
- Chicago plan enthusiasts.
- Benes and Kumhof (2012), Fisher (1936), Simons (1946)
- Narrow banking pro-/op-ponents.
- Kay (2009), Wallace et al. (1996)
- Central bank accounts for all and maturity transformation.
- Fernandez-Villaverde et al. (2020).


## Preview of Results

## What Friction?

- Deposit insurance leads to over-investment.


## Can CBDC Achieve First Best?

- No, if households get paid before the government by defaulting bank.
- Achieves first best if

1. households and government receive money "at the same time" when bank defaults.
2. last dollar of loans receives the output it creates as collateral.

## Preview of Results

Individual uncertainty about timing of consumption (Diamond and Dybvig)


Banking with maturity transformation


Figure 1: Big Picture.

## Outline

## Plan

1. Main Mechanics.
1.1 Derive what governs efficiency in general setup.
1.2 Describe efficiency in different cases.
1.3 Discussion.
2. Big picture.

## Setup

## Basic Setup

- Two periods, household, bank.
- Only household consumes.
- Bank produces and tries to act in household's interest.
- Bank finances itself with deposits (d) and loans (s).


## Setup

## Notation

- What household receives in state $\omega$ if it invests $d$ in deposits and $s$ in loans at interest rates $r$ :

$$
t_{h}(r, s, d, \omega)
$$

- What bank pays in state $\omega$ if it receives $d$ in deposits and $s$ in loans at interest rates $r$ :

$$
t_{b}(r, s, d, \omega)
$$

- Can differ because of deposit insurance.
- Can differ because household gives deposits to government, who hands them on to banks.


## Setup

## What determines level of investment?

- Level of deposits effectively set by government.
- With deposit insurance deposits better for household than loans because insured.
$\Rightarrow$ Free to choose deposits by setting how much deposits are insured.
- With CBDC government sets a different interest rate for household and banks.
$\Rightarrow$ Free to choose deposits by setting interest rate for household.


## Takeaway

- Deposits are effectively fixed.
- Overall investment governed by incentive to invest in loans.


## Money, Money, Money

## Social Planner

- Problem:

$$
u_{0}\left(n_{h}+n_{b}-a\right)+\int u(f(a) \omega) d H(\omega)
$$

- FOC:

$$
u_{0}^{\prime}\left(n_{h}+n_{b}-a\right)=\int u^{\prime}(f(a) \omega) f^{\prime}(a) \omega d H(\omega)
$$

- Look at cases in which FOC is sufficient for optimum.


## Money, Money, Money

## Household

- Problem:

$$
\begin{aligned}
\max _{d, s} u_{0}\left(n_{h}-s-d\right)+\int u\left(t_{h}(r, s, d, \omega)-\tau(\omega)\right. & +\pi(\omega)) d H(\omega) \\
+ & \left\{\lambda\left(\bar{d}-r_{d} d\right)\right\}
\end{aligned}
$$

## Money, Money, Money

## Household

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- FOC:

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u_{0}^{\prime}\left(n_{h}-s-d\right)=\int u^{\prime}(f(a) \omega) \frac{\partial t_{h}(\omega)}{\partial s} d H(\omega)
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## Money, Money, Money

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$$

## Bank

- Problem:

$$
\max _{d^{\prime}, s^{\prime}} u_{0}\left(n_{h}-s-d\right)+\int u\left(\iota(\omega)+f\left(n_{b}+d^{\prime}+s^{\prime}\right) \omega-t_{b}\left(r, s^{\prime}, d^{\prime}, \omega\right)\right) d H(\omega)
$$

## Money, Money, Money

## Household

- Problem:

$$
\begin{aligned}
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- FOC:

$$
\int u^{\prime}(f(a) \omega) \frac{\partial t_{b}(\omega)}{\partial s} d H(\omega)=\int u^{\prime}(f(a) \omega) f^{\prime}(a) \omega d H(\omega)
$$

## Money, Money, Money

## Reminder:

$$
\begin{gathered}
u_{0}^{\prime}\left(n_{h}-s-d\right)=\int u^{\prime}(f(a) \omega) \frac{\partial t_{h}(\omega)}{\partial s} d H(\omega) \\
\int u^{\prime}(f(a) \omega) \frac{\partial t_{b}(\omega)}{\partial s} d H(\omega)=\int u^{\prime}(f(a) \omega) f^{\prime}(a) \omega d H(\omega)
\end{gathered}
$$

## Consequence:

- If $t_{b}^{\prime}(\omega)=t_{h}^{\prime}(\omega)$ we get the efficient outcome.
- If $t_{b}^{\prime}(\omega) \leq t_{h}^{\prime}(\omega)$ and sometimes the equality is strict, then we get over-investment.


## Money, Money, Money

## Important Takeaway:

- Ignore optimization problem. Just look at whether what the household gets from last dollar invested is what the bank pays for it.


## Lemma (Efficiency)

If the planner's problem is convex and the FOCs for loans hold with equality

- the allocation is efficient if $\frac{\partial}{\partial s} t_{b}(\omega)=\frac{\partial}{\partial s} t_{h}(\omega)$
- there is over investment if $\frac{\partial}{\partial s} t_{b}(\omega) \leq \frac{\partial}{\partial s} t_{h}(\omega) \forall \omega$ and the inequality is strict with positive probability
- there is under-investment if $\frac{\partial}{\partial s} t_{b}(\omega) \geq \frac{\partial}{\partial s} t_{h}(\omega) \forall \omega$ and the inequality is strict with positive probability
in equilibrium.


## Results for Baseline

## Baseline

- Deposit insurance.
- Loans are collateralized / have precedence in times of default.


## When are slopes of Transfer functions different?

- $\omega$ such that bank defaults on deposits, not on loans.
- One additional dollar invested in loans receives full interest rate so $t_{h}^{\prime}(\omega)=r_{s}$.
- Bank pays everything it has, so additional payment by bank is $t_{b}^{\prime}(\omega)=f^{\prime}(a) \omega$.
- The second is smaller than the first in default.


## Consequence

- Over-investment.


## Result for CBDC WithOUT Bank Reform

CBDC without bank reform

- In default loans have precedence.

When are slopes of Transfer functions different?

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Consequence

- Over-investment.


## CBDC WithOUT Bank Reform vs Baseline

## Proposition (CBDC without Bank Reform versus Baseline)

If there is an equilibrium with investments $d^{*}, s^{*}$ in the model with deposit insurance for some $\bar{d}$ then for some $r_{d}^{h}$ there is an equilibrium in the model with CBDC for which equilibrium investment is $d^{*}, s^{*}$ and vice versa.

## CBDC With Bank Reform

CBDC with bank reform

- Household and government paid at same time.
- Last dollar of investment receives collateral it creates.

Transfer functions are the same.

- No default: no problem.
- Default on household and central bank:
- Last dollar receives its marginal product as collateral, thus household receives marginal product, and bank pays it.
- $t_{h}^{\prime}(\omega)=t_{b}^{\prime}(\omega)$.
- Bank defaults on government and not on household debt.
- Cannot happen by assumption.


## Consequence

- Efficient solution.


## Is This Feasible?

When do banks default on government and household simultaneously?

- If banks can pledge high quality collateral, then other lenders have precedence over government.
- If banks do maturity transformation, non-government creditors are likely to run first.
- If banks get bailed out when they default this is effectively the same as deposit insurance.
How do we implement optimal bank reform?
- Implementation of optimal bank reform difficult.
- I characterize it, but I do not provide a mechanism (transfer function depends on equilibrium objects).
- But: requiring risky collateral from banks leads to second best.


## Outline

## Plan

1. Main Mechanics.
2. Big picture.

- Model
- Forces
- Outcomes


## Big Picture

Individual uncertainty about timing of consumption (Diamond and Dybvig)


Banking with maturity transformation


Figure 2: Big Picture.

## Model Overview



Figure 3: Model Overview.

- Now two households and two banks.
- Some deposits have precedence in times of default because they are withdrawn.
- Production is linear.


## Equilibrium

## Equilibrium

- In second stage households choose to withdraw deposits maximizing utility.
- In second stage banks maximize value of assets.
- In first stage bank/household optimize as before.


## Second Stage

## Banks in Second Stage

$$
\max _{\Delta} A_{2} \omega\left(a-\frac{1}{A_{1} \omega} \Delta\right)+p \Delta .
$$

- Might already know that they will default, and thus maximize value of their assets.
- Liquidating deposits results in payoff $A_{1}<A_{2}$.
- Equivalent to having banks and households optimize to reinvest deposits.


## Second Stage

## Household Second Stage

$$
\max _{\Delta \in \mathcal{D}} U\left(c_{e}, c_{l}, \psi\right)+\lambda\left(-c_{e}+\Delta\right)+\mu\left(m-p c_{e}-c_{l}\right)
$$

- $0=\psi$ : household only wants to consume late: $U=c_{l}=m$.
- $1=\psi$ : household wants to consume share of its income early until income hits threshold, then wants to consume everything above threshold late.
- Ensures that if limit on $r_{d} d$ high enough there are always enough deposits.
- Ensures that if there is no run only fraction of deposits is withdrawn.
- Scale utility function such that it becomes

$$
U\left(c_{e}(m), c_{l}(m), 1\right)=m
$$

if liquidity constraint does not bind.
$\Rightarrow$ with sufficient deposits liquidity disappears.

## Forces

## Forces in the model

- What banks pay is not what households receive.
- Runs on deposits.


## Forces shut down

- Inefficient incentives of banks who know they will default.
- Runs on anything but deposits.
- Only deposits are run-able (not financial crisis like).
- Avoids that CBDC with bank reform shuts down runs on loans in addition to fixing bank's investment incentives.
- "Collateral externalities" (changing my investment creates/takes away collateral for others/ other types of lending).
- Still anticipate that investing in loans creates collateral that backs these loans.
- Still anticipate that when there's a run on deposits loans might receive zero.


## Outcomes

## No Deposit Insurance

- Keep limit on deposits to make models comparable.
- Set deposits high enough such that liquidity considerations no concern.
- Runs result in effectively lower production.
- If there is a default and banks get run at there might be no deposits left that can be used to pay back loans.
- Slope of transfers paid by bank's sometimes higher than slopes of transfers received by households.
$\Rightarrow$ Lower investment than in planner's problem with inferior production technology.


## Outcomes

## Shrinking the model

- Set level of deposits such that
- there is sufficient liquidity to finance optimal early consumption.
- there are not enough deposits to finance optimal investment.
- Liquidity disappears from the model, and loans determine level of investment.
- Model reduced to the one previously studied (one extra parameter).


## Outcomes

- Deposit insurance $\Rightarrow$ Over-investment.
- CBDC and no bank reform $\Rightarrow$ Over-investment.
- CBDC and bank reform $\Rightarrow$ Optimal allocation.


## Why?

- Same arguments as in first version of the model.


## Outcomes

Leverage constraint and Deposit Insurance

- Two choice variables (loans and deposits), two policy tools (level of deposits, leverage constraint).
- Set deposits to anything that provides sufficient liquidity in every state, and set them lower than optimal investment.
- Set investment using leverage constraint.
$\Rightarrow$ Optimal solution.


## Wrapping Up

## Issues

- Why CBDC if we can use leverage constraints?
- Optimal leverage constraint requires knowledge of optimal investment.
- CBDC requires knowledge about how much liquidity is needed.
$\Rightarrow$ nationalizing liquidity provision lets market set investment.
- Neither CBDC nor leverage constraints without problems.
$\Rightarrow$ Question is which works better.
- Why is CBDC essential? Bank reform without CBDC possible?
- Effectively bank reform without CBDC requires limit on amount of money one can deposit in bank.
- CBDC provides opportunity for bank reform.
- Requiring collateral from banks plausible when CBDC introduced.


## Wrapping Up

## Can CBDC Achieve First Best?

- No, if households get paid before the government by defaulting bank.
- Achieves first best if

1. households and government receive money "at the same time" when bank defaults.
2. last dollar of loans receives the output it creates as collateral.

- First best CBDC
- is not obviously implementable.
- would eliminate chain of inefficiencies and fixes in current system.


## Thank you!

